

Problem 9.4 Solution

Given: The single-story wood-frame warehouse in Fig. 9.B. Roof sheathing of 3/8-in thick 24/0 span-rated STR I sheathing is adequate for vertical "sheathing" loads. Strength level seismic forces to the roof diaphragm are:

$$w_u = w_T = 330 \text{ lb/ft}$$

$$w_u = w_L = 570 \text{ lb/ft}$$

Calculation of unit shears requires consideration of the IBC load combinations. The applicable load combinations from IBC Sec. 1605.3.1 are:

$$D + H + F + (W \text{ or } 0.7E)$$

$$D + H + F + 0.75(W \text{ or } 0.7E) + 0.75 L + 0.75 (L_r \text{ or } S \text{ or } R)$$

$$0.6D + (W \text{ or } 0.7E) + H$$

Because the diaphragm is assumed to only resist horizontal forces, the first and third equations can be simplified to just "0.7E." The redundancy / reliability factor will be assumed to be 1.0.

a. Design the roof diaphragm, considering lateral forces in both directions. Show all criteria including design shears, load cases, allowable shears, and nailing requirements. If blocking is required, determine at what points it can be omitted.

Transverse Direction Unit Shears

$$w_T = 330 \text{ plf}$$

$$R = V = 330 \text{ plf } (120 \text{ ft } / 2) = 19,800 \text{ lb}$$

$$b = 70 \text{ ft}$$

$$v = V/b = 19,800 \text{ lb } / 70 \text{ ft} = 283 \text{ plf strength}$$

$$= 198 \text{ plf ASD}$$

Longitudinal Direction Unit Shears

$$w_L = 570 \text{ plf}$$

$$R = V = 570 \text{ plf } (70 \text{ ft } / 2) = 19,950 \text{ lb}$$

$$b = 120 \text{ ft}$$

$$v = V/b = 19,950 \text{ lb } / 120 \text{ ft} = 166 \text{ plf strength}$$

$$= 116 \text{ plf ASD}$$

Diaphragm Aspect Ratio

Per IBC Table 2305.2.3, for unblocked wood structural panel diaphragms the maximum allowable span to width ratio is 3:1, while for blocked diaphragms it is

4:1. The actual maximum span-to-width ratio for this diaphragm is 120 ft / 70 ft = 1.7, which is less than either maximum allowable, so OK.

Actual versus Allowable Shears

Transverse Loading. From IBC Table 2306.3.1, the panel layout and load direction for transverse loading correspond to Case 1. For 3/8 inch Structural I sheathing, 2x framing members, and an unblocked diaphragm, the allowable Case 1 shear using 8d common nails is 240 plf, which is greater than the 198 plf ASD demand. Transverse loading does not require blocking.

Longitudinal Loading. From IBC Table 2306.3.1, the panel layout and load direction for transverse loading correspond to Case 3. For 3/8 inch Structural I sheathing, 2x framing members, and an unblocked diaphragm, the allowable Case 3 shear is 180 plf, which is greater than the 116 plf ASD demand. Blocking is not required for longitudinal loading.

Diaphragm nailing requirements

- 8 common nails – unblocked diaphragm
- 8d @ 6" oc supported edges
- 8d @ 12" oc other supports (field nailing)

b. Calculate the maximum chord forces for both lateral force directions. Also, calculate the chord forces at the ends of all headers in the exterior walls.

Transverse Loading

Mid-Span

$$M_u = \frac{w_r L^2}{8} = \frac{330(120)^2}{8} = 594,000 \text{ lb-ft} = 594 \text{ kip-ft}$$

$$T_u = \frac{M_u}{b} = \frac{594 \text{ kip-ft}}{70 \text{ ft}} = 8.49 \text{ kips}$$

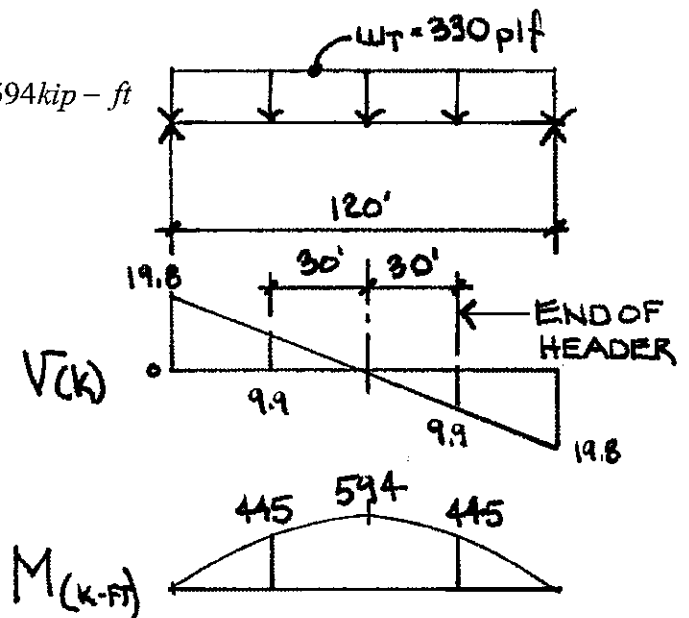
$$T = 0.7(T_u) = 0.7(8.49) = 5.94 \text{ kips}$$

End of Header

$$M_u = \frac{(19.8 + 9.9k)(30 \text{ ft})}{2} = 445 \text{ kip-ft}$$

$$T_u = \frac{M_u}{b} = \frac{445 \text{ kip-ft}}{70 \text{ ft}} = 6.36 \text{ kips}$$

$$T = 0.7(T_u) = 0.7(6.36) = 4.45 \text{ kips}$$



Longitudinal Loading

West Wall

Mid-Span

$$M_u = \frac{w_L L^2}{8} = \frac{570(70)^2}{8} = 349,000 \text{ lb-ft} = 349 \text{ kip-ft}$$

$$T_u = \frac{M_u}{b} = \frac{349 \text{ kip-ft}}{120 \text{ ft}} = 2.91 \text{ kips}$$

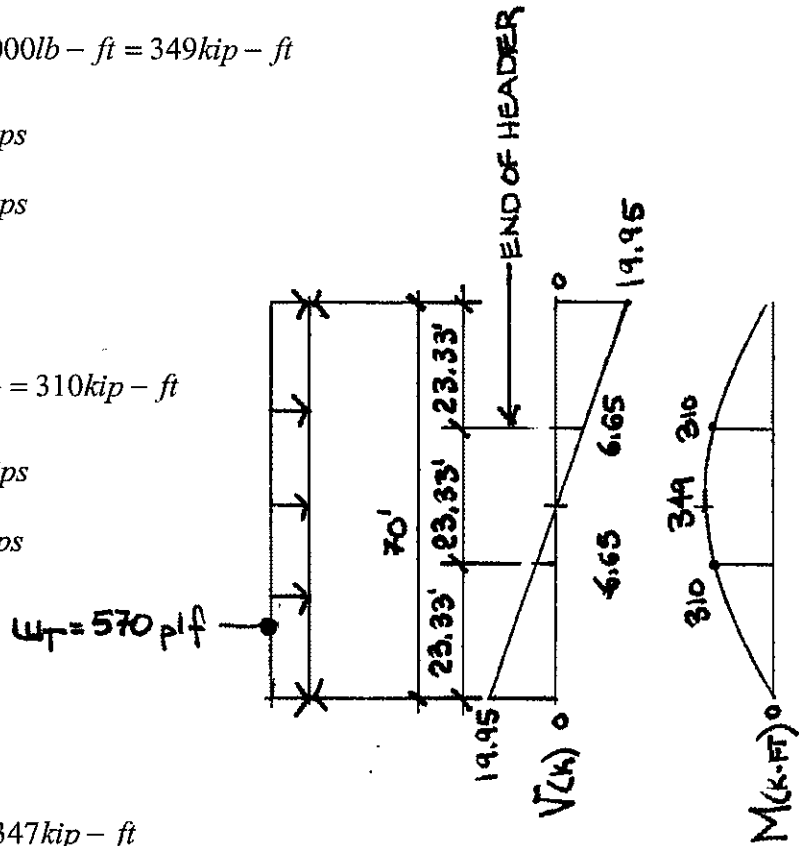
$$T = 0.7(T_u) = 0.7(2.91) = 2.04 \text{ kips}$$

End of Header

$$M_u = \frac{(19.95 + 6.65k)(23.33 \text{ ft})}{2} = 310 \text{ kip-ft}$$

$$T_u = \frac{M_u}{b} = \frac{310 \text{ kip-ft}}{120 \text{ ft}} = 2.58 \text{ kips}$$

$$T = 0.7(T_u) = 0.7(2.58) = 1.81 \text{ kips}$$



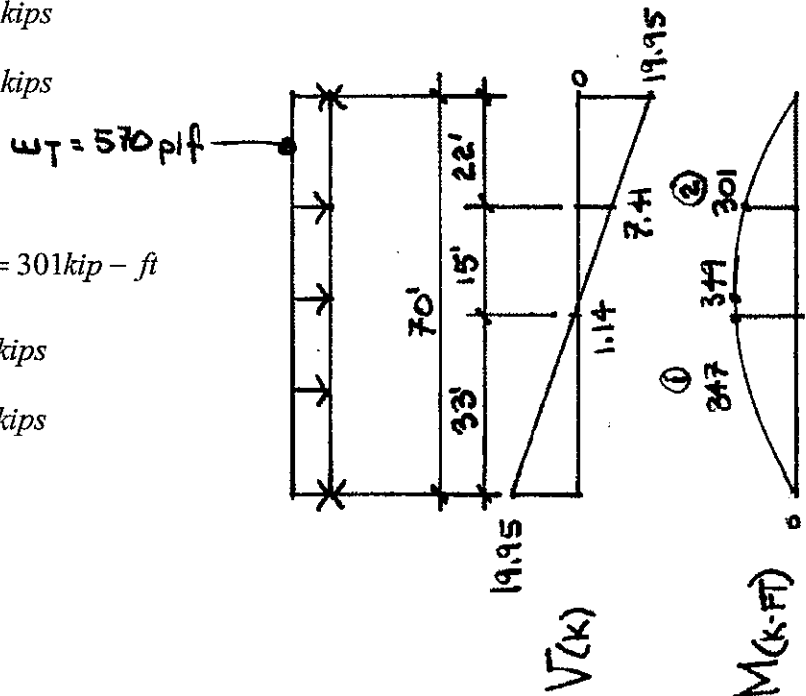
East Wall

End of Header 1

$$M_u = \frac{(19.95 + 1.14k)(33 \text{ ft})}{2} = 347 \text{ kip-ft}$$

$$T_u = \frac{M_u}{b} = \frac{347 \text{ kip-ft}}{120 \text{ ft}} = 2.89 \text{ kips}$$

$$T = 0.7(T_u) = 0.7(2.89) = 2.02 \text{ kips}$$



End of Header 2

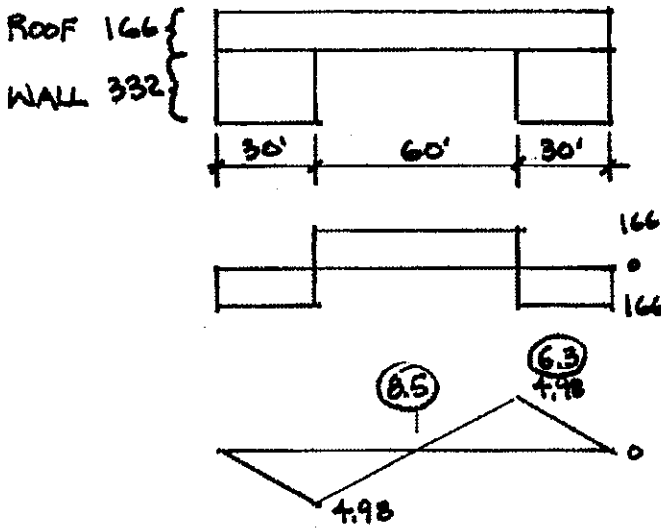
$$M_u = \frac{(19.95 + 7.41k)(22 \text{ ft})}{2} = 301 \text{ kip-ft}$$

$$T_u = \frac{M_u}{b} = \frac{301 \text{ kip-ft}}{120 \text{ ft}} = 2.51 \text{ kips}$$

$$T = 0.7(T_u) = 0.7(2.51) = 1.76 \text{ kips}$$

c. Plot the distribution of the collector (strut) force for each of the walls with openings. Compare the collector (strut) forces and chord forces to determine the critical loading.

SOUTH WALL



$$\text{WALL UNIT SHEAR} = \frac{19950\#}{60'} = 332 \text{ plf}$$

$$\text{ROOF UNIT SHEAR} = \frac{19950\#}{120'} = 166 \text{ plf}$$

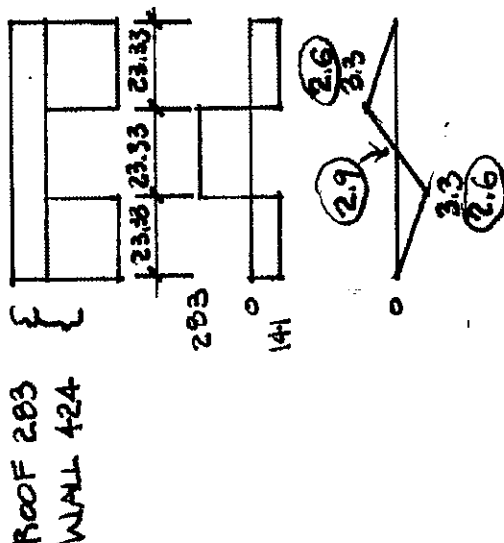
UNIT SHEARS (PLF)

NET UNIT SHEARS (PLF)

STRENGTH LEVEL
 COLLECTOR FORCE (K)
 (CHORD FORCES SHOWN IN
 CIRCLES FOR COMPARISON)

SOUTH WALL MAX
 FORCE = 8.5K
 CHORD
 NORTH WALL SAME

WEST WALL

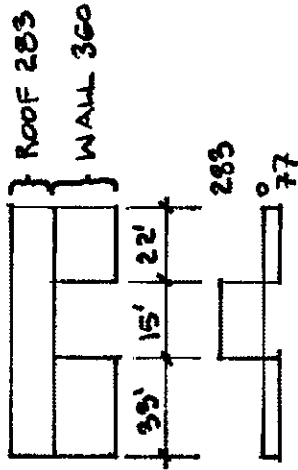


$$\text{WALL UNIT SHEAR} = \frac{19800}{46.7} = 424 \text{ plf}$$

$$\text{ROOF UNIT SHEAR} = \frac{19800}{70} = 283 \text{ plf}$$

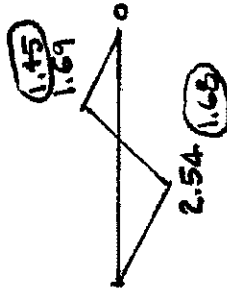
WEST WALL MAX
 FORCE = 3.3K
 CHORD

EAST WALL



UNIT SHEARS (PIF)

NET UNIT SHEARS (PIF)



COLLECTOR FORCE (k)
 (CHORD FORCE
 IN CIRCLE)

$$\text{WALL UNIT SHEAR} = \frac{19800}{55'} = 360 \text{ pif}$$

$$\text{ROOF UNIT SHEAR} = \frac{19800}{70'} = 283 \text{ pif}$$

EAST WALL MAX
 FORCE = 2.54 k STR
 CHORD

Problem 9.10 Solution

Given: The one-story building in Fig. 9.D. Roof sheathing is 15/32-in. 32/16 span-rated panels spanning between roof joists spaced 24 in oc. Nails are 10d common. For the transverse strength level seismic force, the panel layout is load case 1.

a. Design the roof diaphragm assuming that only the exterior walls are effective in resisting the lateral force. Show all design criteria including span-width ratio, nailing, and blocking requirements. Omit blocking where possible. Do not consider deflection of the diaphragm.

Calculation of critical lateral forces requires consideration of the IBC load combinations. The applicable load combinations from IBC Sec. 1605.3.1 are:

$$\begin{aligned}
 &D + H + F + (W \text{ or } 0.7E) \\
 &D + H + F + 0.75(W \text{ or } 0.7E) + 0.75L + 0.75(L_r \text{ or } S \text{ or } R) \\
 &0.6D + (W \text{ or } 0.7E) + H
 \end{aligned}$$

Because the diaphragm is assumed to only resist horizontal forces, the first and third equations can be simplified to just "0.7E." The redundancy / reliability factor will be assumed to be 1.0.

$$\begin{aligned}
 w_T = w_L &= 335 \text{ plf Strength} \\
 &= 0.7(335) = 235 \text{ plf ASD}
 \end{aligned}$$

Transverse Loading

$$\begin{aligned}
 w_T &= 235 \text{ plf} \\
 R = V &= 235 \text{ plf} (110 \text{ ft} / 2) = 12,920 \text{ lb} \\
 b &= 50 \text{ ft} \\
 v = V/b &= 12,920 \text{ lb} / 50 \text{ ft} = 258 \text{ plf}
 \end{aligned}$$

Span to Width ratio = 110 ft / 50 ft = 2.2. This is less than the 3.0 permitted by IBC Table 2305.2.3.

From IBC Table 2306.3.1, for 15/32 inch rated sheathing, unblocked with 10d nails, the allowable Case 1 shear is 255 plf. Because this is approximately equal to the 258 plf demand, blocking will not be required.

b. Redesign the roof diaphragm, assuming that the interior and exterior walls are effective shearwalls. Show all criteria except deflection.

Transverse Loading

Use tributary area method, design diaphragm for longer 80 ft span.

$$\begin{aligned}w_T &= 235 \text{ plf} \\R = V &= 235 \text{ plf} (80 \text{ ft} / 2) = 9400 \text{ lb} \\b &= 50 \text{ ft} \\v &= V/b = 9400 \text{ lb} / 50 \text{ ft} = 188 \text{ plf}\end{aligned}$$

Span to Width ratio = 80 ft / 50 ft = 1.6. This is less than the 3.0 permitted by IBC Table 2305.2.3.

From IBC Table 2306.3.1, for 15/32 inch rated sheathing, unblocked with 10d nails, the allowable Case 1 shear is 255 plf. Because this is less than the 188 plf demand, blocking will not be required.

c. Compare the maximum chord forces for a and b.

Chord - Transverse Loading, 110 ft span

$$M = \frac{w_T L^2}{8} = \frac{235(110)^2}{8} = 355,000 \text{ lb-ft} = 355 \text{ kip-ft}$$

$$T = \frac{M}{b} = \frac{355 \text{ kip-ft}}{50 \text{ ft}} = 7.1 \text{ kips ASD}$$

Chord - Transverse Loading, 80 ft span

$$M = \frac{w_T L^2}{8} = \frac{235(80)^2}{8} = 188,000 \text{ lb-ft} = 188 \text{ kip-ft}$$

$$T = \frac{M}{b} = \frac{188 \text{ kip-ft}}{50 \text{ ft}} = 3.8 \text{ kips ASD}$$

d. Plot the collector force diagram for the interior shearwall.

ROOF SHEAR $V_1 = \frac{235 \text{ plf} (30/2 \text{ ft})}{50} = 71 \text{ plf}$
 $V_2 = 188 \text{ plf}$

WALL SHEAR $V = \frac{235 \text{ plf} (110/2 \text{ ft})}{30} = 431 \text{ plf}$

